

Code: ME7T3

**IV B.Tech - I Semester – Regular/Supplementary Examinations
October - 2019**

**FINITE ELEMENT METHODS
(MECHANICAL ENGINEERING)**

Duration: 3 hours

Max. Marks: 70

PART – A

Answer *all* the questions. All questions carry equal marks

11 x 2 = 22 M

1. a) What is plane stress condition?
- b) What are the equations of equilibrium for 3-D body?
- c) Define minimum potential energy principle.
- d) What is isoparametric representation? Briefly explain.
- e) Define bandwidth of a stiffness matrix.
- f) What is CST? Why it is named as CST?
- g) Write the relation for Jacobian transformation of triangular element?
- h) What is axi symmetric loading?
- i) Explain about Hermite shape functions with neat sketches.
- j) Specify the boundary conditions for steady state heat transfer problem.
- k) Differentiate Local and Global coordinate systems incase of truss elements.

PART – B

Answer any **THREE** questions. All questions carry equal marks.

$$3 \times 16 = 48 \text{ M}$$

2. a) Derive the equilibrium equations for three dimensional stress system of rectangular element and tetrahedral element. 12 M

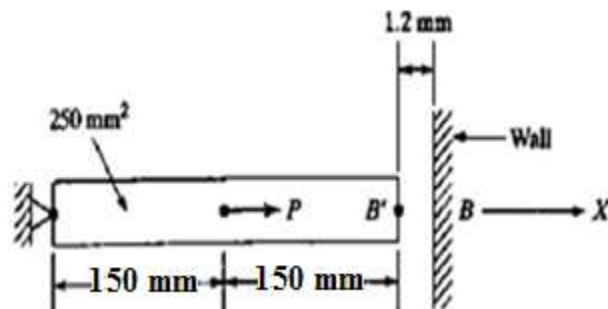
b) If a displacement field is described by 4 M

$$u = (-2x + 3y^2 + xy)10^{-4} \text{ and } v = (x^2 + 5y - y^2)10^{-4}$$

Determine ϵ_x , ϵ_y , and ϵ_{xy} at the point $x = 2$, $y = 1$.

3. Determine the displacements, stress and support reactions in the structure shown in the figure. 16 M

Take $P = 62 \times 10^3 \text{ N}$, $E = 20 \times 10^3 \text{ N/mm}^2$, $A = 250 \text{ mm}^2$

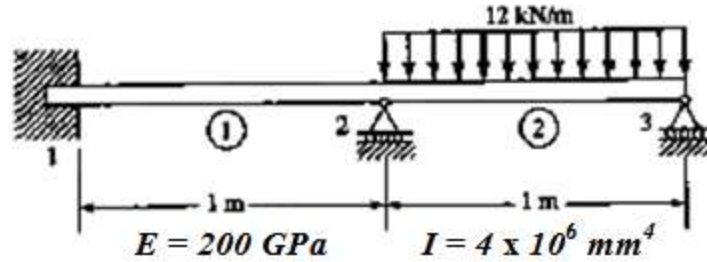


4. a) Derive the stiffness matrix for a truss element. 6 M

b) For the beam as shown in figure, determine 10 M

i) The slopes at 2 and 3 and

ii) Vertical deflection at the midpoint of the distributed load.



5. a) Derive the element strain displacement matrix for three noded CST element. 8 M

b) Calculate the element stiffness matrix of a CST element under plane stress condition with vertices 1(0,0), 2(300,0) and 3(300, 200) mm. Take $E = 300 \text{ GPa}$ and $\nu = 0.25$. Thickness of the element is 10 mm. 8 M

6. A long hollow cylinder of inside diameter 100mm and outside diameter 120mm is firmly fitted in a hole of another rigid cylinder over its full length as shown in fig. The cylinder is then subjected to an internal pressure of 2 MPa. By using two elements on the 10mm length, calculate the displacements at the inner radius. Take $E = 210 \text{ GPa}$. $\nu = 0.3$. 16 M

